

$$(1) \int \frac{5}{y^6} dy = -\frac{1}{y^5} + C$$

$$(2) \int x^2 \sqrt{x} dx = \int x^{\frac{5}{2}} dx$$

$$= \frac{2}{7} x^{\frac{7}{2}} + C$$

$$= \frac{2}{7} x^3 \sqrt{x} + C$$

$$(3) \int \frac{\sqrt{x}-1}{\sqrt[3]{x}} dx = \int (x^{\frac{1}{6}} - x^{-\frac{1}{3}}) dx$$
$$= \frac{6}{7} x^{\frac{7}{6}} - \frac{3}{2} x^{\frac{2}{3}} + C$$
$$= \frac{6}{7} \sqrt[6]{x^7} - \frac{3}{2} \sqrt[3]{x^2} + C$$

$$(4) \int \frac{2x^3 - x^2 + 3x - 1}{x^2} dx = \int (2x - 1 + \frac{3}{x} - \frac{1}{x^2}) dx$$
$$= x^2 - x + 3 \log|x| + \frac{1}{x} + C$$

$$(5) \int \sqrt{x} \left(1 + \frac{1}{\sqrt{x}}\right)^2 dx = \int \sqrt{x} \left(1 + \frac{2}{\sqrt{x}} + \frac{1}{x}\right) dx$$
$$= \int (\sqrt{x} + 2 + \frac{1}{\sqrt{x}}) dx$$
$$= \frac{2}{3} \sqrt{x^3} + 2x + 2\sqrt{x} + C$$

$$(6) \int (5 \sin x - 4 \cos x) dx = -5 \cos x - 4 \sin x + C$$

$$(7) \int \left(\frac{1}{\tan x} + 2\right) \sin x dx = \int (\cos x + 2 \sin x) dx$$
$$= \sin x - 2 \cos x + C$$

$$(8) \int (2e^x - x^2) dx = 2e^x - \frac{1}{3} x^3 + C$$

$$(9) \int (5^x - e^x) dx$$
$$= \frac{5^x}{\log 5} - e^x + C$$

$$(10) \int \left(2e^x + \frac{3}{x}\right) dx$$
$$= 2e^x + 3 \log|x| + C$$